



Mark Scheme (Results)

October 2020

Pearson Edexcel IAL Mathematics (WMA12)
Pure Mathematics P2

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

General Instructions for Marking

1. The total number of marks for the paper is 75.
2. The Pearson Mathematics mark schemes use the following types of marks:
 - **M** marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
 - **A** marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
 - **B** marks are unconditional accuracy marks (independent of M marks)
 - Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used if you are using the annotation facility on ePEN.

- bod – benefit of doubt
 - ft – follow through
 - the symbol \surd or ft will be used for correct ft
 - cao – correct answer only
 - cso - correct solution only. There must be no errors in this part of the question to obtain this mark
 - isw – ignore subsequent working
 - awrt – answers which round to
 - SC: special case
 - oe – or equivalent (and appropriate)
 - d... or dep – dependent
 - indep – independent
 - dp decimal places
 - sf significant figures
 - * The answer is printed on the paper or ag- answer given
 - \square or d... The second mark is dependent on gaining the first mark
4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected. If you are using the annotation facility on ePEN, indicate this action by 'MR' in the body of the script.
6. If a candidate makes more than one attempt at any question:
 - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
 - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
7. Ignore wrong working or incorrect statements following a correct answer.
8. Marks for each question are scored by clicking in the marking grids that appear below each student response on ePEN. The maximum mark allocation for each question/part question(item) is set out in the marking grid and you should allocate a score of '0' or '1' for each mark, or "trait", as shown:

	0	1
aM		•
aA	•	
bM1		•
bA1	•	
bB	•	
bM2		•
bA2		•

9. Be careful when scoring a response that is either all correct or all incorrect. It is very easy to click down the '0' column when it was meant to be '1' and all correct.

General Principles for Core Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

Method mark for solving 3 term quadratic:

1. Factorisation

$$(x^2 + bx + c) = (x + p)(x + q), \text{ where } |pq| = |c|, \text{ leading to } x = \dots$$

$$(ax^2 + bx + c) = (mx + p)(nx + q), \text{ where } |pq| = |c| \text{ and } |mn| = |a|, \text{ leading to } x = \dots$$

2. Formula

Attempt to use correct formula (with values for a , b and c).

3. Completing the square

$$\text{Solving } x^2 + bx + c = 0: \quad (x \pm \frac{b}{2})^2 \pm q \pm c, \quad q \neq 0, \quad \text{leading to } x = \dots$$

Method marks for differentiation and integration:

1. Differentiation

Power of at least one term decreased by 1. ($x^n \rightarrow x^{n-1}$)

2. Integration

Power of at least one term increased by 1. ($x^n \rightarrow x^{n+1}$)

Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

Method mark for quoting a correct formula and attempting to use it, even if there are small mistakes in the substitution of values.

Where the formula is not quoted, the method mark can be gained by implication from correct working with values, but may be lost if there is any mistake in the working.

Exact answers

Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

Answers without working

The rubric says that these may not gain full credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required. Most candidates do show working, but there are occasional awkward cases and if the mark scheme does not cover this, please contact your team leader for advice.

Question Number	Scheme	Notes	Marks
1(a)	$\left(2 - \frac{x}{4}\right)^{10} = 2^{10} + \binom{10}{1}2^9\left(-\frac{x}{4}\right) + \binom{10}{2}2^8\left(-\frac{x}{4}\right)^2 + \binom{10}{3}2^7\left(-\frac{x}{4}\right)^3 + \dots$ <p>Attempts the binomial expansion to get the third and/or fourth term with an acceptable structure. The correct binomial coefficient must be combined with the correct power of $\frac{x}{4}$ and the correct power of 2 but condone omission of brackets.</p> <p>You can ignore the signs between the terms and allow the terms to be listed.</p> <p>Allow for e.g. $\pm \binom{10}{2}2^8\left(\pm\frac{x}{4}\right)^2$ or $\pm^{10}C_32^7\left(\pm\frac{x}{4}\right)^3$ but condone omission of brackets.</p> <p>NB $^{10}C_2 = 45$, $^{10}C_3 = 120$ NB $^{10}C_2 = ^{10}C_8$ and $^{10}C_3 = ^{10}C_7$</p> <p>Alternative:</p> $\left(2 - \frac{x}{4}\right)^{10} = 2^{10}\left(1 - \frac{x}{8}\right)^{10} = 2^{10}\left(1 - \frac{10x}{8} + \frac{10 \times 9}{2}\left(-\frac{x}{8}\right)^2 + \frac{10 \times 9 \times 8}{3!}\left(-\frac{x}{8}\right)^3 + \dots\right)$ <p>Score M1 for $2^{10}\left(\dots \pm \frac{10 \times 9}{2}\left(-\frac{x}{8}\right)^2 + \dots\right)$ or $2^{10}\left(\dots \pm \frac{10 \times 9 \times 8}{3!}\left(-\frac{x}{8}\right)^3 + \dots\right)$</p>		M1
	$= 1024 - 1280x + 720x^2 - 240x^3$	1024 – 1280x	B1
		720x ² or –240x ³	A1
		720x ² and –240x ³	A1
	Note that if any of the “–”s are “+ –”s then penalise once on the first occurrence		
	<p>Allow the terms to be listed e.g. 1024, –1280x, 720x², –240x³</p> <p>Apply isw once a correct answer is seen.</p> <p>Ignore any extra terms</p>		
		(4)	
(b)	$\left(3 - \frac{1}{x}\right)^2 = 9 - \frac{6}{x} + \frac{1}{x^2}$ or $9 - \frac{3}{x} - \frac{3}{x} + \frac{1}{x^2}$	Correct expansion. May be implied by their work to find the constant.	B1
	$\left(3 - \frac{1}{x}\right)^2 \left(2 - \frac{x}{4}\right)^{10} = \left(9 - \frac{6}{x} + \frac{1}{x^2}\right) (1024 - 1280x + 720x^2 - 240x^3 + \dots)$ <p>constant term = $9 \times 1024 - \frac{6}{x}(-1280x) + \frac{1}{x^2}720x^2$</p> <p>This mark depends on having obtained an expression of the form $A + \frac{B}{x} + \frac{C}{x^2}$ for $\left(3 - \frac{1}{x}\right)^2$ and at least a 3-term quadratic expression from part (a) so award for: $A \times "1024" + B \times "-1280" + C \times "720"$ A, B, C non-zero. Allow 1 sign error on their values.</p> <p>May be seen as part of a complete expansion but there must be an attempt to calculate the value of the constant term with the above conditions. For reference, true value calculation is: 9216 + 7680 + 720</p>		M1
	$= 17616$	Correct value. Must be “extracted” if a complete expansion is found above.	A1
			(3)
		Total 7	

Question Number	Scheme						Notes	Marks
2(a)	x	- 0.25	0	0.25	0.5	0.75		B1
	y	0.462	0.577	0.653	0.686	0.698		
	<p>Allow awrt these values and look for the values appearing in the body of the script or within their calculation in part (b).</p> <p>Also allow exact value for the 0.577 e.g. $\frac{1}{\sqrt{3}}$ or $\frac{\sqrt{3}}{3}$</p>							(1)
(b)	$h = 0.25$						Correct strip width. May be implied by $\frac{1}{8}$ or $\frac{1}{2} \times 0.25$	B1
	$A \approx \frac{1}{2} \times "0.25" \{0.462 + 0.698 + 2("0.577" + 0.653 + "0.686")\}$ <p>Correct application of the trapezium rule with their h Must be a correct application of the rule so e.g.</p> $A \approx \frac{1}{2} \times "0.25" \times 0.462 + 0.698 + 2("0.577" + 0.653 + "0.686")$ <p>Scores M0 unless any missing brackets are implied by subsequent work.</p> $A \approx \frac{1}{2} \times "0.25" \{0.462 + 0.698 + 2("0.577" + 0.653 + "0.686")\}$ <p>Would also score M0 unless the closing bracket was implied by subsequent work Condone copying slips e.g. 0.426 instead of 0.462. Must use all the y-values. Repeated or missing y-values scores M0. Allow separate trapezia e.g.</p> $A \approx \frac{1}{2} \times "0.25" (0.462 + "0.577") + \frac{1}{2} \times "0.25" ("0.577" + 0.653) + \frac{1}{2} \times "0.25" (0.653 + "0.686") + \frac{1}{2} \times "0.25" ("0.686" + 0.698)$ <p>Allow use of the function e.g.</p> $A \approx \frac{1}{2} \times 0.25 \left\{ \frac{2^{-0.25}}{\sqrt{5(-0.25)^2 + 3}} + \frac{2^{0.75}}{\sqrt{5(0.75)^2 + 3}} + 2 \left(\frac{2^0}{\sqrt{5(0)^2 + 3}} + \frac{2^{0.25}}{\sqrt{5(0.25)^2 + 3}} + \frac{2^{0.5}}{\sqrt{5(0.5)^2 + 3}} \right) \right\}$						M1	
	= awrt 0.624 or $\frac{78}{125}$ oe e.g. $\frac{312}{500}$						accept awrt 0.624 or exact fraction but isw if necessary	A1
	Note that the calculator answer for the integral is 0.6265569683...							(3)
							Total 4	

Question Number	Scheme	Notes	Marks
3(a)	$a(-4)^3 - (-4)^2 + b(-4) + 4 = -108$ <p>Attempts to set $f(-4) = -108$ to obtain an equation in a and b. Score when you see “- 4” embedded in the equation or 2 correct terms (excluding the “+ 4”) on lhs. May be implied by e.g. $-64a - 16 - 4b + 4 = -108$ Condone minor slips on the lhs e.g. one sign error between terms but must use $- 108$</p>		M1
	<p>As an alternative for the first mark we will condone an attempt at long division. This requires a complete method to divide $(ax^3 - x^2 + bx + 4)$ by $(x + 4)$ to obtain a remainder in terms of a and b which is then equated to -108 For reference, the quotient is $ax^2 - (1+4a)x + 16a + b + 4$ and the remainder is $-4b - 64a - 12$</p>		
	$-64a - 16 - 4b + 4 = -108$ $\Rightarrow 16a + b = 24^*$	<p>Correct equation obtained with no errors and at least one line of intermediate working if starting with e.g.</p> $a(-4)^3 - (-4)^2 + b(-4) + 4 = -108$	A1*
			(2)
(b)	$a\left(\frac{1}{2}\right)^3 - \left(\frac{1}{2}\right)^2 + b\left(\frac{1}{2}\right) + 4 = 0$ <p>Attempts to set $f\left(\frac{1}{2}\right) = 0$ to obtain an equation in a and b. Condone slips. Score when you see “$\frac{1}{2}$” embedded in the equation or 2 correct terms (excluding the “+ 4”) on lhs. May be implied by e.g. $\frac{a}{8} - \frac{1}{4} + \frac{b}{2} + 4 = 0$ The “= 0” may be implied when they attempt to solve simultaneously below</p>		M1
	<p>An alternative for the first mark is to attempt long division. This requires a complete method to divide $(ax^3 - x^2 + bx + 4)$ by $(2x - 1)$ to obtain a remainder in a and b which is then equated to 0 For reference, the quotient is $\frac{a}{2}x^2 + \left(\frac{a}{4} - \frac{1}{2}\right)x + \left(\frac{b}{2} - \frac{1}{4} + \frac{a}{8}\right)$ and the remainder is $\frac{15}{4} + \frac{b}{2} + \frac{a}{8}$</p>		
	$16a + b = 24, a + 4b = -30$ $\Rightarrow a = \dots, b = \dots$	<p>Attempts to solve $16a + b = 24$ simultaneously with their equation in a and b. This may be implied if values of a and b are obtained (e.g. calculator)</p>	M1
	$a = 2, b = -8$	<p>Correct values</p>	A1
			(3)
(c)	$f(x) = 2x^3 - x^2 - 8x + 4$ $\Rightarrow f'(x) = 6x^2 - 2x - 8$	<p>Correct derivative (follow through their a and b). Allow unsimplified and apply isw if necessary. Allow with the letters “a” and “b” and a “made up” “a” and “b”.</p>	B1ft
			(1)

(d)	$6x^2 - 2x - 8 = 0$ $\Rightarrow (3x - 4)(x + 1) = 0$ $\Rightarrow x = \dots$	Sets their $f'(x) = 0$ (may be implied) and solves a 3 term quadratic. Apply general guidance if necessary. You may need to check if a calculator has been used.	M1
	$x = \frac{4}{3}, -1 \Rightarrow y = \dots$	Uses at least one of their x values to find a value for y using their $f(x)$ <u>where x is from an attempt to solve $f'(x) = 0$</u> . You may need to check their y values if working is not shown.	M1
	$\left(\frac{4}{3}, -\frac{100}{27}\right) \text{ or } (-1, 9)$ <p>Or e.g. $x = \frac{4}{3}, y = -\frac{100}{27}$ and $x = -1, y = 9$</p> <p>One correct point. The fractional coordinates must be exact but allow 1.3 with a dot over the 3 and 3.703 with dots over the 7 and 3. Note that it is not necessary for the points to be written as coordinates as long as the pairing is clear.</p> <p>Depends on having scored both previous M marks.</p>		A1
	$\left(\frac{4}{3}, -\frac{100}{27}\right) \text{ and } (-1, 9)$ <p>Or e.g. $x = \frac{4}{3}, y = -\frac{100}{27}$ and $x = -1, y = 9$</p> <p>Both correct points. The fractional coordinates must be exact but allow 1.3 with a dot over the 3 and 3.703 with dots over the 7 and 3. Note that it is not necessary for the points to be written as coordinates as long as the pairing is clear.</p> <p>Depends on having scored both previous M marks.</p>		A1
	<p>Fully correct answers with no working scores 4/4 following a <u>correct</u> part (c) i.e.</p> $\Rightarrow f'(x) = 6x^2 - 2x - 8$		
			(4)
			Total 10

Question Number	Scheme	Notes	Marks
4(a)(i)	(-7, 9) or e.g. $x = -7, y = 9$	$x = -7$ or $y = 9$	B1
		$x = -7$ and $y = 9$	B1
	Award the marks in (a) once correct answers are seen. Special case: If all you see is (9, -7) award B1B0		
(a)(ii)	<u>Examples:</u> $r = \sqrt{(-3 - (-7))^2 + (12 - 9)^2}$ <p style="text-align: center;">or</p> $r = \sqrt{(-11 - (-7))^2 + (6 - 9)^2}$ <p style="text-align: center;">or</p> $r = \frac{1}{2} \sqrt{(-3 + 11)^2 + (12 - 6)^2}$	Correct strategy for the radius. Must be a correct method for their centre (if used) but allow 1 sign slip within one of the brackets . A correct answer scores both marks. Must see the $\frac{1}{2}$ if finding the length of the diameter.	M1
	$r = 5$	Correct radius	A1
(b)	$(x + 7)^2 + (y - 9)^2 = 5^2$ <p style="text-align: center;">or e.g.</p> $x^2 + y^2 + 2 \times 7x - 2 \times 9y + 7^2 + 9^2 - 5^2 = 0$ <p style="text-align: center;">M1: Correct attempt at circle equation using their values. Allow for</p> $(x \pm (\text{their } 7))^2 + (y \pm (\text{their } 9))^2 = (\text{their numerical } r)^2$ <p style="text-align: center;">or e.g.</p> $x^2 + y^2 \pm 2 \times (\text{their } 7)x \pm 2 \times (\text{their } 9)y + (\text{their } 7)^2 + (\text{their } 9)^2 - (\text{their numerical } r)^2 = 0$ <p style="text-align: center;">A1: Correct equation in any form</p>		M1A1
			(2)
(c)	$m_{\text{radius}} = \frac{12 - 9}{-3 + 7} \left(= \frac{3}{4} \right) \text{ or}$ $m_{\text{tangent}} = -1 \div \left(\frac{12 - 9}{-3 + 7} \right) \left(= -\frac{4}{3} \right) \text{ or}$ $m_{\text{tangent}} = - \left(\frac{-3 + 7}{12 - 9} \right) \left(= -\frac{4}{3} \right)$	This mark is for an attempt to find the radius gradient or the tangent gradient. If the method is not clear allow one sign error in the numerator or denominator.	M1
	<p style="text-align: center;">Alternative for the first M:</p> $(x + 7)^2 + (y - 9)^2 = 5^2 \Rightarrow 2(x + 7) + 2(y - 9) \frac{dy}{dx} = 0$ $\frac{dy}{dx} = \frac{x + 7}{9 - y} = \frac{-3 + 7}{9 - 12} \left(= -\frac{4}{3} \right)$ <p style="text-align: center;">Allow for $(x + 7)^2 + (y - 9)^2 = 5^2 \Rightarrow \alpha(x + 7) + \beta(y - 9) \frac{dy}{dx} = 0 \Rightarrow \frac{dy}{dx} = \dots$</p>		
	$y - 12 = -\frac{4}{3}(x + 3)$ <p>Uses a correct straight line method for the tangent using the point Q. Must be fully correct work here so must be a clear attempt at the tangent not the radius. So if the radius gradient is found previously, must apply negative reciprocal rule to their radius gradient. If using $y = mx + c$ must reach as far as $c = \dots$</p>		M1
	$4x + 3y - 24 = 0$	Allow any integer multiple	A1
			(3)
			Total 9

Question Number	Scheme	Notes	Marks
5(a)	$t_{40} = 100 + (40 - 1) \times 5$	Uses $a + (n - 1)d$ with $a = 100$, $d = 5$ and $n = 40$. This may be implied by a correct expression e.g. $100 + 39 \times 5$	M1
	$= (\pounds)295$	Cao. Correct answer with no working scores both marks.	A1
			(2)
(b)	$S_{60} = \frac{1}{2}(60)(2 \times 100 + (60 - 1) \times 5)$ or $l = 100 + (60 - 1) \times 5 = 395$ $S_{60} = \frac{1}{2}(60)(100 + 395)$	Uses a correct sum formula with $a = 100$, $d = 5$ and $n = 60$ or $n = 40$. May be implied by a correct numerical expression. If using $\frac{1}{2}n(a + l)$ with $n = 40$ you may see $\frac{1}{2}(40)(100 + 295)$ using their result from (a) and this scores M1 also.	M1
		Correct numerical expression with $n = 60$. If there are any missing brackets then this mark should be withheld unless the correct expression is implied by their answer.	A1
	$= (\pounds)14\ 850$	Cao. Correct answer with no working scores 3 marks. Apply isw if necessary and award this mark once a correct answer is seen.	A1
			(3)
(c)	$\frac{1}{2}n(2 \times 600 + (n - 1) \times -10) = 18200$	Attempts to use a correct sum formula with $a = 600$, $d = -10$ and sets = 18 200. Condone poor use of brackets.	M1
		Correct equation which may be implied by subsequent work.	A1
	$600n - 5n^2 + 5n = 18200$ $5n^2 - 605n + 18200 = 0$ $n^2 - 121n + 3640 = 0^*$	Obtains the printed answer with at least one intermediate line and no errors. Allow other variables to be used for n but the final answer must be as printed including “= 0”	A1*
			(3)
(d)	$(n - 56)(n - 65) = 0$ $\Rightarrow (n =) 56, 65$	Attempts to solve the given quadratic. This may be implied by correct answers. Apply general guidance if necessary but must reach at least one value for n . (Allow them to use x rather than n)	M1
		Correct values (ignore how they are labelled e.g. allow $x = \dots$)	A1
			(2)
(e)	E.g. $(n =) 65$ because e.g. the money has already been saved after 56 months	States $(n =) 65$ and gives a suitable reason – see below for examples of acceptable comments. There must be no contradictory statements and any calculations must be correct.	B1
			(1)
			Total 11

Acceptable comments for 5(e):

$n = 65$ means $t = 600 - 10 \times 64 = -40$ which is not possible/doesn't make sense/etc.

$n = 65$ because Lina will have saved the money after 56 months

$n = 65$ because Lina will have saved the money before then

$600 + (n - 1) \times -10 = 0 \Rightarrow n = 61$ so she will have paid off the loan before $n = 65$

Condone “because $65 > 60$ ” or equivalent e.g. it is only over 60 months (or 5 years)

$n = 65$ means $t = 600 - 10 \times 64 = -40$ so reject (but not just “it is negative”)

(b)	$x^n \rightarrow x^{n+1}$	For increasing any power of x by 1 for C_1 or C_2 or for $\pm (C_1 - C_2)$	M1
$\pm \int \{-2x^2 + 7x - 1 - (x^3 - 6x + 9)\} dx = \pm \int (-x^3 - 2x^2 + 13x - 10) dx$ $= \pm \left(-\frac{x^4}{4} - \frac{2x^3}{3} + \frac{13x^2}{2} - 10x \right)$ <p style="text-align: center;">or</p> $\pm \left\{ \int (-2x^2 + 7x - 1) dx - \int (x^3 - 6x + 9) dx \right\}$ $= \pm \left(-\frac{2x^3}{3} + \frac{7x^2}{2} - x - \left(\frac{x^4}{4} - \frac{6x^2}{2} + 9x \right) \right)$ <p style="text-align: center;">or</p> $\int (-2x^2 + 7x - 1) dx = -\frac{2x^3}{3} + \frac{7x^2}{2} - x, \quad \int (x^3 - 6x + 9) dx = \frac{x^4}{4} - \frac{6x^2}{2} + 9x$		dM1A1	
<p style="text-align: center;">dM1: For correct integration of 1 term for C_1 and one term for C_2 or for correct integration for 2 terms of <u>their</u> $\pm (C_1 - C_2)$</p> <p style="text-align: center;">A1: Fully correct integration of both C_1 and C_2 or for $\pm (C_1 - C_2)$. Award this mark as soon as fully correct integration is seen and ignore subsequent work.</p>		$= -\frac{2^4}{4} - \frac{2(2)^3}{3} + \frac{13(2)^2}{2} - 10(2) - \left(-\frac{1^4}{4} - \frac{2(1)^3}{3} + \frac{13(1)^2}{2} - 10(1) \right)$	ddM1
$= \frac{13}{12}$		<p style="text-align: center;">Fully correct strategy for the area. Depends on both previous M marks. Uses the limits "2" and 1 in their "changed" expression(s) and subtracts either way round.</p>	A1
			(5)
Total 9			

Some values for reference:

$$\left[\frac{-2x^3}{3} + \frac{7x^2}{2} - x \right]_1^2 = \frac{20}{3} - \frac{11}{6} = \frac{29}{6} \quad \left[\frac{x^4}{4} - \frac{6x^2}{2} + 9x \right]_1^2 = 10 - \frac{25}{4} = \frac{15}{4}$$

$$= -\frac{2^4}{4} - \frac{2(2)^3}{3} + \frac{13(2)^2}{2} - 10(2) - \left(-\frac{1^4}{4} - \frac{2(1)^3}{3} + \frac{13(1)^2}{2} - 10(1) \right) = -\frac{10}{3} - \left(-\frac{53}{12} \right)$$

Question Number	Scheme	Notes	Marks
7(i)	$\tan \theta + \frac{1}{\tan \theta} = \frac{\sin \theta}{\cos \theta} + \frac{1}{\frac{\sin \theta}{\cos \theta}}$ <p style="text-align: center;">or</p> $\tan \theta + \frac{1}{\tan \theta} = \frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{\sin \theta}$	Uses $\tan \theta \equiv \frac{\sin \theta}{\cos \theta}$ on both terms	M1
	$\frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{\sin \theta} = \frac{\sin^2 \theta + \cos^2 \theta}{\sin \theta \cos \theta} \quad \text{or} \quad \frac{\sin^2 \theta}{\sin \theta \cos \theta} + \frac{\cos^2 \theta}{\sin \theta \cos \theta}$ <p>Uses $\tan \theta \equiv \frac{\sin \theta}{\cos \theta}$ and $\frac{1}{\tan \theta} \equiv \frac{\cos \theta}{\sin \theta}$ and attempts common denominator of $\sin \theta \cos \theta$ with a 2 term numerator one of which is correct. Or attempts 2 separate fractions with a denominator of $\sin \theta \cos \theta$ one of which is correct. Depends on the first mark.</p>		dM1
	$= \frac{1}{\sin \theta \cos \theta} *$ <p style="text-align: center;">or</p> $\frac{1}{\cos \theta \sin \theta}$	Correct proof with no notation errors or missing variables but allow “ \equiv ” instead of “ $=$ ”. If there are any spurious “ $= 0$ ”s alongside the proof score A0.	A1*
			(3)
Alternative 1 for (i)			
	$\tan \theta + \frac{1}{\tan \theta} = \frac{\tan^2 \theta + 1}{\tan \theta} \left(\text{or } \frac{\tan^2 \theta}{\tan \theta} + \frac{1}{\tan \theta} \right)$	Attempts common denominator of $\tan \theta$	M1
	$= \frac{\sec^2 \theta}{\tan \theta} = \frac{1}{\cos^2 \theta} \times \frac{\cos \theta}{\sin \theta}$ <p style="text-align: center;">Or</p> $= \frac{\frac{\sin^2 \theta}{\cos^2 \theta} + 1}{\frac{\sin \theta}{\cos \theta}} = \frac{1}{\cos^2 \theta} \times \frac{\cos \theta}{\sin \theta}$	Applies appropriate and correct identities to obtain in terms of $\sin \theta$ and $\cos \theta$ only and eliminates “double decker” fractions if necessary	dM1
	$= \frac{1}{\sin \theta \cos \theta} *$ <p style="text-align: center;">or</p> $\frac{1}{\cos \theta \sin \theta}$	Correct proof with no notation errors or missing variables but allow “ \equiv ” instead of “ $=$ ”. If there are any spurious “ $= 0$ ”s alongside the proof score A0.	A1*
Alternative 2 for (i)			
	$\tan \theta + \frac{1}{\tan \theta} = \frac{1}{\sin \theta \cos \theta} \Rightarrow \frac{\sin^2 \theta}{\cos \theta} + \cos \theta = \frac{1}{\cos \theta}$ <p>Uses $\tan \theta \equiv \frac{\sin \theta}{\cos \theta}$ and multiplies through by $\sin \theta$ or $\cos \theta$</p>		M1
	$\Rightarrow \sin^2 \theta + \cos^2 \theta = 1$ <p>Uses $\tan \theta \equiv \frac{\sin \theta}{\cos \theta}$ and multiplies through by $\sin \theta$ and $\cos \theta$</p>		dM1
	$\sin^2 \theta + \cos^2 \theta = 1$ is true hence proved	Fully correct work reaching a correct identity with a conclusion. If there are any spurious “ $= 0$ ”s alongside the proof score A0.	A1*

(ii)	$3 \cos^2(2x + 10^\circ) = 1 \Rightarrow \cos^2(2x + 10^\circ) = \frac{1}{3} \Rightarrow \cos(2x + 10^\circ) = (\pm) \sqrt{\frac{1}{3}}$ <p>Divides by 3 and takes square root of both sides. The “±” is not required.</p>		M1
	$2x + 10^\circ = \cos^{-1} \left(\left(\pm \right) \sqrt{\frac{1}{3}} \right)$ $\Rightarrow x = \frac{\cos^{-1} \left(\left(\pm \right) \sqrt{\frac{1}{3}} \right) - 10^\circ}{2}$	$\cos^{-1} \left(\left(\pm \right) \sqrt{\frac{1}{3}} \right) \pm 10^\circ$ <p>Applies $x = \frac{\cos^{-1} \left(\left(\pm \right) \sqrt{\frac{1}{3}} \right) \pm 10^\circ}{2}$</p> <p>You may need to check their values if no working is shown.</p>	M1
	For reference $2x + 10^\circ = 54.735\dots, 125.264\dots$		
	$x = 22.4^\circ$ or $x = 57.6^\circ$	Awrt one of these	A1
	$x = 22.4^\circ$ and $x = 57.6^\circ$	Awrt both with no extras in range	A1
	If mixing degrees and radians allow the method marks.		
			(4)
Alternative 1 for part (b)			
$3 \cos^2(2x + 10^\circ) = 1 \Rightarrow 3(1 - \sin^2(2x + 10^\circ)) = 1 \Rightarrow$ $\Rightarrow \sin^2(2x + 10^\circ) = \frac{2}{3} \Rightarrow \sin(2x + 10^\circ) = (\pm) \sqrt{\frac{2}{3}}$ <p>Uses a correct identity, rearranges and takes square root of both sides. The “±” is not required.</p>		M1	
$2x + 10^\circ = \sin^{-1} \left(\left(\pm \right) \sqrt{\frac{2}{3}} \right)$ $\Rightarrow x = \frac{\sin^{-1} \left(\left(\pm \right) \sqrt{\frac{2}{3}} \right) - 10^\circ}{2}$	$\sin^{-1} \left(\left(\pm \right) \sqrt{\frac{2}{3}} \right) \pm 10^\circ$ <p>Applies $x = \frac{\sin^{-1} \left(\left(\pm \right) \sqrt{\frac{2}{3}} \right) \pm 10^\circ}{2}$</p> <p>You may need to check their values if no working is shown.</p>	M1	
$x = 22.4^\circ$ or $x = 57.6^\circ$	Awrt one of these	A1	
$x = 22.4^\circ$ and $x = 57.6^\circ$	Awrt both with no extras in range	A1	
Alternative 2 for part (b)			
$3 \cos^2(2x + 10^\circ) = 3 \left(\frac{1 + \cos(4x + 20^\circ)}{2} \right) \Rightarrow \cos(4x + 20^\circ) = -\frac{1}{3}$ <p>Uses a correct identity, rearranges to make $\cos(4x + 20^\circ)$ the subject</p>		M1	
$2x + 10^\circ = \cos^{-1} \left(-\frac{1}{3} \right)$ $\Rightarrow x = \frac{\cos^{-1} \left(-\frac{1}{3} \right) - 20^\circ}{4}$	$\cos^{-1} \left(-\frac{1}{3} \right) - 20^\circ$ <p>Applies $\Rightarrow x = \frac{\cos^{-1} \left(-\frac{1}{3} \right) - 20^\circ}{4}$</p> <p>You may need to check their values if no working is shown.</p>	M1	
For reference $4x + 20^\circ = 109.47\dots, 250.52\dots$			
$x = 22.4^\circ$ or $x = 57.6^\circ$	Awrt one of these	A1	
$x = 22.4^\circ$ and $x = 57.6^\circ$	Awrt both with no extras in range	A1	
		Total 7	

Question Number	Scheme	Notes	Marks
8(a)	$S_n = a + ar + \dots + ar^{n-1}$ $rS_n = ar + ar^2 + \dots + ar^n$	Writes down at least 3 correct terms of a geometric series and multiplies their sequence by r . There may be extra incorrect terms but allow this mark if there are 3 correct terms in both sequences and at least one "+" in both sequences but see special case below	M1
	$S_n - rS_n = a - ar^n \quad \text{or} \quad rS_n - S_n = ar^n - a$	Obtains either equation where both S_n and rS_n had the correct first and last terms and at least one other correct term but no incorrect terms. Both sides must be seen unfactorised.	A1(M1 on EPEN)
	$(1-r)S_n = a(1-r^n) \Rightarrow S_n = \frac{a(1-r^n)}{1-r} *$ <p>Factorises both sides and divides by $1-r$ to obtain the printed answer</p> <p>Should be as printed but allow e.g. $S_n = \frac{a(1-r^n)}{(1-r)}$ but not $S_n = \frac{a(r^n-1)}{(r-1)}$ unless followed by correct version</p>		A1*
	<p align="center">Special case:</p> <p align="center">If terms are listed rather than added and the working is otherwise correct score 110</p> <p align="center">See next page for proof by induction.</p>		(3)
Alternative for (a):			
	$S_n = a + ar + \dots + ar^{n-1}$ $(1-r)S_n = (1-r)(a + ar + \dots + ar^{n-1}) \quad \text{or} \quad S_n = \frac{(1-r)(a + ar + \dots + ar^{n-1})}{(1-r)}$	Writes down at least 3 correct terms of a geometric series and multiplies both sides by $1-r$ or multiplies the right hand side by $\frac{1-r}{1-r}$	M1
	$(1-r)S_n = a - ar^n \quad \text{or} \quad S_n = \frac{a - ar^n}{1-r}$	Obtains the above equation where S_n had the correct first and last terms and at least one other correct term and no incorrect terms. Right hand side must be seen unfactorised unless the "a" was factored out earlier	A1 (M1 on EPEN)
	$(1-r)S_n = a - ar^n = a(1-r^n) \Rightarrow S_n = \frac{a(1-r^n)}{1-r} *$ <p align="center">or</p> $S_n = \frac{a - ar^n}{1-r} \Rightarrow S_n = \frac{a(1-r^n)}{1-r} *$	Should be as printed but allow e.g. $S_n = \frac{a(1-r^n)}{(1-r)}$ but not $S_n = \frac{a(r^n-1)}{(r-1)}$ unless followed by correct version	A1*

(b)	Mark (b) and (c) together		
	$r^3 = -\frac{20.48}{320} \Rightarrow r = \sqrt[3]{-\frac{20.48}{320}}$	Correct strategy for r . Allow for dividing the 2 given terms either way round and attempting to cube root.	M1
	$= -0.4$	Correct value (and no others) but allow equivalents e.g. $-2/5$. Correct answer only scores both marks.	A1
	<p>Note that some candidates take $ar^2 = -320$ and $ar^5 = \frac{512}{25}$ and use these correctly to give</p> $r^3 = -\frac{20.48}{320} \Rightarrow r = \sqrt[3]{-\frac{20.48}{320}} = -0.4$ <p style="text-align: center;">In such cases you can allow full marks for (b) but see note * in (c)</p>		
		(2)	

(c)	$r = -0.4 \Rightarrow a = \frac{-320}{-0.4} (= 800)$ or $r = -0.4 \Rightarrow a = \frac{512}{25} \div \left(-\frac{2}{5}\right)^4 (= 800)$	Correct attempt at the first term using \pm their r and the -320 or the $\frac{512}{25}$. May be implied by their a but must be using e.g. $ar = -320$ or $ar^4 = \frac{512}{25}$ not $ar^2 = -320$ or $ar^5 = \frac{512}{25}$ *	M1
	$S_{13} = \frac{"800"(1 - "-0.4"^{13})}{1 - "-0.4"}$ <p>Correct attempt at the sum using their a and their r and $n = 13$ to find a value for S_{13}. <u>Must be a fully correct attempt at the sum here using $n = 13$, their a and their r.</u></p> <p>Note that $\frac{800(1 + 0.4^{13})}{1 + 0.4}$ is equivalent to $\frac{800(1 - (-0.4)^{13})}{1 - (-0.4)}$ and is acceptable for this mark.</p>		M1
	$= 571.43$	Correct value. Note that S_{∞} is also 571.43 so working must be seen i.e. correct answer only scores no marks.	A1
			(3)
		Total 8	

Proof by induction for part (a):

$$n = 1 \Rightarrow S_1 = \frac{a(1-r^1)}{1-r} = a \text{ so true for } n = 1$$

$$\text{Assume true for } n = k \text{ so } S_k = \frac{a(1-r^k)}{1-r}$$

$$\begin{aligned} \text{Add } (k+1)^{\text{th}} \text{ term } S_{k+1} &= \frac{a(1-r^k)}{1-r} + ar^k = \frac{1-ar^k + ar^k - ar^{k+1}}{1-r} \\ &= \frac{a - ar^{k+1}}{1-r} = \frac{a(1-r^{k+1})}{1-r} \end{aligned}$$

So if true for $n = k$ it has been shown true for $n = k + 1$ and as it is true for $n = 1$ it is true for (for all n)

Mark as follows:

M1: Shows true for $n = 1$ and assumes true for $n = k$ and adds the $(k+1)^{\text{th}}$ term

A1(M1 on EPEN): Finds common denominator obtains $\frac{a - ar^{k+1}}{1-r}$ using correct algebra

A1: Fully correct proof reaching $\frac{a(1-r^{k+1})}{1-r}$ with all steps shown and conclusion

If you are in any doubt about awarding marks in this case or any other cases that you think deserve credit, send to your Team Leader using Review

Question Number	Scheme	Notes	Marks	
9(i)	$4 = \log_3 81$ or $4 = \log_3 3^4$ May be implied by e.g. $\log_3 \frac{x+5}{2x-1} = 4 \Rightarrow \frac{x+5}{2x-1} = 3^4$ (or 81)		B1	
	Examples: $\log_3(x+5) - \log_3 81 = \log_3 \frac{x+5}{81}$ or $\log_3(x+5) - \log_3(2x-1) = \log_3 \frac{x+5}{2x-1}$ or $\log_3(2x-1) + \log_3 81 = \log_3 81(2x-1)$ This mark is for combining 2 log terms correctly and can be awarded following an incorrect rearrangement e.g. $\log_3(x+5) - 4 = \log_3(2x-1) \Rightarrow \log_3(x+5) + \log_3(2x-1) = 4$ $\Rightarrow \log_3(2x-1)(x+5) = \dots$		M1	
	$\frac{x+5}{81} = 2x-1$	Obtains this equation in any form e.g. $\frac{x+5}{2x-1} = 3^4$	A1	
	$x = \frac{86}{161}$	Cao	A1	
	Condone the omission of the base throughout			
				(4)
	Alternative for first 3 marks: $\log_3(x+5) - 4 = \log_3(2x-1) \Rightarrow 3^{\log_3(x+5)-4} = 3^{\log_3(2x-1)}$ $\Rightarrow 3^{\log_3(x+5)} \times 3^{-4} = 2x-1 \Rightarrow \frac{x+5}{81} = 2x-1$ Score B1 for sight of 3^{-4} and M1 for applying $3^{a \pm b} = 3^a \times 3^{\pm b}$ and A1 as above			
	(a) Special Case $\log_3(x+5) - \log_3(2x-1) = 4 \Rightarrow \frac{\log_3(x+5)}{\log_3(2x-1)} = 4 \Rightarrow \frac{x+5}{2x-1} = 81 \Rightarrow x = \frac{86}{161}$ Scores B1(implied) M0 A0 A1			
(ii)(a)	$3^{y+3} = 3^y \times 3^3$ or $2^{1-2y} = 2 \times 2^{-2y}$ or $\frac{2}{2^{2y}}$ or 2×4^{-y} or $\frac{2}{4^y}$	One correct index law seen or implied anywhere in their working	B1	
	$3^{y+3} \times 2^{1-2y} = 27 \times 3^y \times 2 \times 2^{-2y} = \dots$	Applies both correct index laws to the lhs of the equation	M1(B1 on EPEN)	
	$3^y \times 2^{-2y} = \frac{108}{27 \times 2}$ or $\frac{3^y}{4^y} = \frac{108}{27 \times 2}$ or $\frac{3^y}{2^{2y}} = \frac{108}{54}$ Isolates the terms in y (as powers of 3 and 2(or 4)) on the lhs and the constants on the rhs. There must be no incorrect work to combine terms e.g. $3^y \times 3^3 = 27^y$ etc.		M1	
	$(0.75)^y = 2^*$	Cso. Reaches the given answer with no errors and all steps shown with 2^{2y} appearing as 4^y at some point.	A1*	
				(4)

	Alternative 1 for (ii)(a) using logs:		
	$\log(3^{y+3} \times 2^{1-2y}) = \log 3^{y+3} + \log 2^{1-2y}$ Or $\log 3^{y+3} = (y+3)\log 3$ Or $\log 2^{1-2y} = (1-2y)\log 2$	One correct log law seen or implied anywhere in their working. No bracketing errors allowed for <u>this mark</u>.	B1
	$\log 3^{y+3} + \log 2^{1-2y} = (y+3)\log 3 + (1-2y)\log 2$ Applies the correct log laws to the lhs. You can condone missing brackets around the $y+3$ and/or $1-2y$		M1(B1 on EPEN)
	$(y+3)\log 3 + (1-2y)\log 2 = \log 108 \Rightarrow \log 3^y - \log 2^{2y} = \log 108 - 3\log 3 - \log 2$ $\Rightarrow \log \frac{3^y}{2^{2y}} = \log \frac{108}{3^3 \times 2}$ Proceeds to isolate the terms in y on the lhs and combines the constants on the rhs or e.g. $(y+3)\log 3 + (1-2y)\log 2 = \log 108 \Rightarrow y(\log 3 - 2\log 2) = \log \frac{108}{3^3 \times 2}$ Proceeds to isolate the terms in y on the lhs and combines the constants on the rhs		M1
	$(0.75)^y = 2^*$	Cso. With e.g. $2\log 2$ seen as $\log 4$ or $\log 2^2$ or implied at some point.	A1*
	Alternative 2 for (ii)(a) using factors of 108:		
	$3^{y+3} \times 2^{1-2y} = 108 = 2^2 \times 3^3$ $\Rightarrow \frac{3^{y+3} \times 2^{1-2y}}{2^2 \times 3^3} = \dots$ $\Rightarrow 3^y \times 2^{-1-2y} = \dots$	One correct index law seen or implied anywhere in their working e.g. $\frac{3^{y+3}}{3^3} = 3^y$ or $\frac{2^{1-2y}}{2^2} = 2^{-1-2y}$	B1
	$\Rightarrow 3^y \times 2^{-1-2y} = \dots$	Applies both correct index laws to the lhs of the equation	M1(B1 on EPEN)
	$\Rightarrow 3^y \times 2^{-2y} = 2$	Proceeds to isolate the terms in y (as powers of 3 and 2(or 4)) on the lhs and the constants on the rhs	M1
	$(0.75)^y = 2^*$	Cso. Reaches the given answer with no errors and all steps shown with 2^{2y} appearing as 4^y at some point.	A1*
(b)	$(0.75)^y = 2 \Rightarrow y = \frac{\log 2}{\log 0.75}$ or $(0.75)^y = 2 \Rightarrow y = \log_{0.75} 2$	Correct processing to obtain a value for y May be implied by awrt - 2.4	M1
	$y = -2.409$	Awrt -2.409 A correct answer implies both marks	A1
			(2)
			Total 10

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